

Course on Energy Economics

# Theoretical Analysis of Competition and Market Power in Wholesale Electricity Markets

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# Motivation

The **absence of market power**, a necessary condition for efficiency

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- ▶ Different types of market organizations, or '**market designs**', give rise to different types of strategic opportunities for exercising market power.
- ▶ An **understanding of how market power will be exercised** in any particular market requires an understanding of the strategies available to firms, and an equilibrium analysis of the market game being played.

# Outline

1. Supply Function Model
2. Multi-Unit Auction Model
  - ▶ Symmetric duopoly
  - ▶ Asymmetric duopoly
  - ▶ Symmetric Oligopoly

# The Supply Function Approach

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  - ▶ Each firm has a **set of profit maximizing points**, one corresponding to each realization of its residual demand.
  - ▶ If firms must decide on their strategies in advance of the realization of demand, then they are better off specifying an entire supply curve.



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  - ▶ If firms must decide on their strategies in advance of the realization of demand, then they are better off specifying an entire supply curve.
- ▶ Green and Newbery (1992) observed that demand uncertainty in K&M is formally identical to **demand variation** over time when firms' bids remain valid for a given period of time.

# Model Description I

- ▶ Two symmetric firms,  $i = 1, 2$ .
- ▶ Demand  $D(p, t)$ : known; decreasing and concave in  $p$ , varies over  $t$ .
- ▶ Cost  $C(q)$ : non-decreasing and convex,  $C'(p) \geq 0$  and  $C''(p) > 0$ .

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- ▶ Supply functions  $S_i(p)$ : continuously differentiable and non-decreasing.
- ▶ The auctioneer determines the lowest price  $p^*$  such that each firm produces over its supply function and the market clears,  $S_1(p^*) + S_2(p^*) = D(p^*, t)$ .

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- ▶ A **Nash equilibrium in supply functions** is a supply function pair  $\{S_1(p), S_2(p)\}$  such that  $S_i(p)$  maximizes  $i$ 's expected profits given  $S_j(p)$ .
- ▶ **Market clearing** implies firms produce on their Residual Demand,

$$q_i(t) = S_i(p) = D(p, t) - S_j(p).$$

## Model Description II

- ▶ Firm  $i$ 's profits are given by

$$\pi_i(p, t) = p [D(p, t) - S_j(p)] - C_i(D(p, t) - S_j(p)).$$

## Model Description II

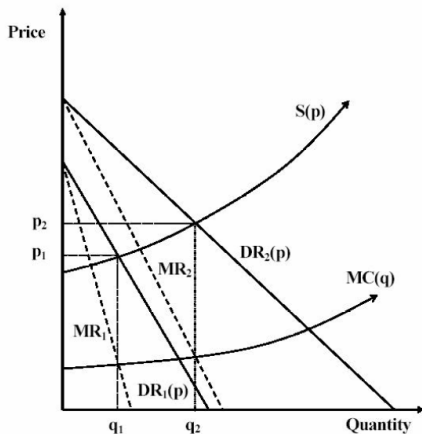
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- ▶ Assuming that  $i$ 's set of ex-post profit maximizing points can be described as a supply function which intersects each realisation of  $i$ 's residual demand curve once and only once,
  - ▶ e.g.  $RD$  curves shift in a parallel fashion,
- ▶ ...firm  $i$ 's profit maximization problem can be expressed as

$$\max_p \pi_i(p, t) .$$

# Optimal Supply Function



Source: Frank Wolak

## Model Description III

- ▶ Differentiating profits w.r.t.  $p$  yields the FOC:

$$\frac{dq_j}{dp} = \frac{q_j}{p - C'(q_j)} + D_p$$

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- ▶ Supply functions must be non-decreasing, so that  $\frac{dq}{dp} \in (0, \infty)$ , or

$$C'(q) < p < C'(q) - \frac{q}{D_p}$$

# Results I

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## Bounds:

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- ▶ If firm  $j$  has an unresponsive output  $k_j$ :

$$\pi_i(p, t) = p [D(p, t) - k_j] - C_i(D(p, t) - k_j).$$

$$FOC : q_i + [p - C'(q_i)] D_p = 0 \Rightarrow p = C'(q) - \frac{q}{D_p}$$

## Results II

- ▶ For a given price, there is **continuum of possible supply functions** supporting it.
  - ▶ If **demand is certain** (i.e., no demand variation), each firm's residual demand is also certain. Thus, there is a single price-quantity pair that max. its profits.
  - ▶ Hence, **whatever supply function passing through it, is ex-post optimal** as all other points in its supply function will not be reached in equilibrium.

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  - ▶ If **demand can be arbitrarily high** with some probability (i.e. if the support of the random variable is unbounded), there is a **unique equilibrium**.
    - ▶ As the FOC has to be satisfied at infinitely many points, there is only one such supply function passing through them all.

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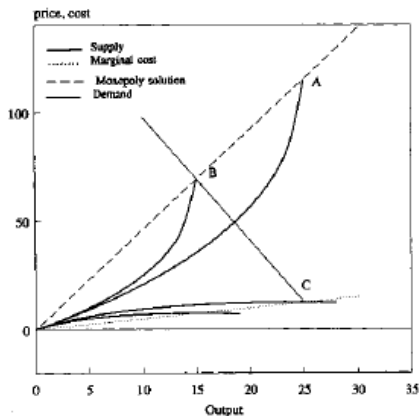
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  - ▶ If **demand can be arbitrarily high** with some probability (i.e. if the support of the random variable is unbounded), there is a **unique equilibrium**.
    - ▶ As the FOC has to be satisfied at infinitely many points, there is only one such supply function passing through them all.
  - ▶ In all intermediate case, there is a **connected set of equilibria** lying between the perfectly competitive and the Cournot solutions.
  - ▶ Some authors restrict attention to **linear supply functions**,  $S(p) = A - bp$ , as there is a unique equilibrium in linear functions-intuition: there is unique line connecting (at least) two ex-post price-quantity pairs.

# Feasible Supply Function Equilibria



Source: Green and Newbery (JPE, 1992)

# Discussion

- ▶ If the range of variation in demand is finite then the model appears to have **little predictive value**:
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- ▶ If the (short-run) elasticity of **demand for electricity is zero** then the model has no solution in the sense that the Cournot solution is undefined.
- ▶ The assumption that generators submit **continuously differentiable supply functions** is contrary to reality:
  - ▶ Original market design in England and Wales: generators were allowed to submit up to three incremental prices per unit
  - ▶ Spain: firms are allowed to submit up to 25 price-quantity pairs per unit.

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  - ▶ Original market design in England and Wales: generators were allowed to submit up to three incremental prices per unit
  - ▶ Spain: firms are allowed to submit up to 25 price-quantity pairs per unit.
- ▶ Further, this assumption yields equilibria which do not exist in models in which **generating units are discrete...**

# Main References

-  Akgün, U. (2004) “Mergers with Supply Functions,” *Journal of Industrial Economics*, 52(4).
-  Baldwin et al. (2004) “Theory and Application of Linear Supply Function Equilibrium in Electricity Markets,” *Journal of Regulatory Economics*, 25.
-  Delgado, J. (2006) “Coalition-proof supply function equilibria under capacity constraints,” *Economic Theory* 29(1), 219-229.
-  \* Green, R. and D. Newbery (1992) “Competition in the British Electricity Spot Market,” *Journal of Political Economy* 100(5), 929-53.
-  Klemperer, P. and M. Meyer (1989) “Supply Function Equilibria in Oligopoly under Uncertainty,” *Econometrica* 57(6), 1243-77.

# Model Description I

## Duopoly

- ▶ two symmetric suppliers (extension to  $N \geq 2$  asymmetric firms)
- ▶ (fixed) capacity constraints  $k$  (extension to endogenous capacities)
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## Bids

- ▶ each supplier makes one bid  $(b_1, b_2)$  (extension to multi-units)
- ▶ constrained by “market reserve price”  $P$

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## Price formation

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$$q_i(\theta; \mathbf{b}) = \begin{cases} \min\{\theta, k\} & \text{if } b_i < b_j \\ \frac{1}{2} \min\{\theta, k\} + \frac{1}{2} \max\{0, \theta - k\} & \text{if } b_i = b_j \\ \max\{0, \theta - k\} & \text{if } b_i > b_j \end{cases}$$

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- ▶ both firms are paid at the highest accepted bid (“System Marginal Price”)

$$p^* = \begin{cases} b_j & \text{if } b_i \leq b_j \text{ and } \theta > k; \\ b_i & \text{otherwise} \end{cases}$$

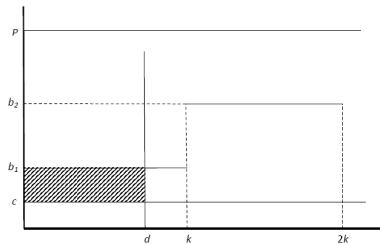


Figure 1: Low demand  $\theta < k$

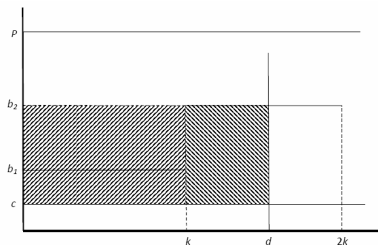


Figure 2: High demand  $\theta > k$

# Equilibrium prices and profits

## Proposition

*(i) (Low demand) if  $\theta \leq k$ , in the unique pure-strategy equilibrium the highest accepted price offer equals  $c$  and suppliers make no profits.*

*(ii) (High demand) if  $\theta > k$ , in any pure-strategy equilibrium one firm bids at  $P$  whereas the rival submits bids no greater than  $c + [P - c] [\theta - k] / \theta$ . The high-bidding supplier makes profits  $[P - c] [\theta - k]$  whereas the low-bidding supplier makes profits  $[P - c] k$ .*

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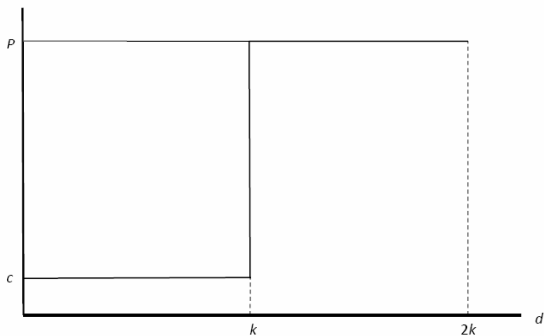


Figure 3: Equilibrium prices as a function of demand



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$$\pi_i(b) = F_j(b) (b - c) [\theta - k] + k \int_b^P (v - c) dF_j(v)$$

- ▶ On  $(\underline{b}, P)$ , the net gain from raising the bid must be zero:

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- ▶ *Price effect*: increasing the bid increases profits if the rival bids below,  $F(b) [\theta - k]$ , but
- ▶ *Quantity effect*: reduces the prob. of selling at capacity instead of residual demand,  $-f(b) (b - c) [k - (\theta - k)]$ .

# Mixed Strategy Equilibrium

- ▶ We need to solve a differential equation:

$$F(b) [\theta - k] - f(b) (b - c) [k - (\theta - k)] = 0$$

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- ▶ Equilibrium profits become:  $\pi = (P - c) [\theta - k]$

# Empirical Evidence: UK Pool

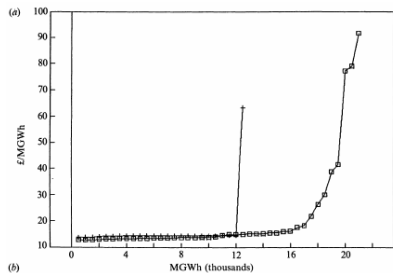


Figure 4: Low demand

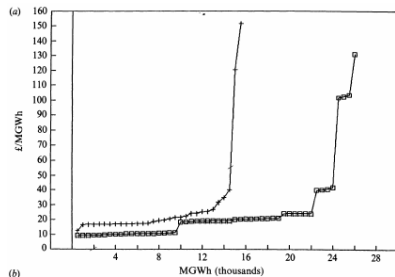


Figure 5: High demand

Source: von der Fehr and Harbord (EJ, 1993)

# Asymmetric Capacities and Symmetric Costs

- ▶ Assume (possibly) asymmetric capacities  $k_1 \geq k_2$  [firm 1 large]

## Proposition

(i) (Low demand) if  $\theta \leq k_2$ , in the unique pure-strategy equilibrium the highest accepted price offer equals  $c$  and suppliers make no profits.

(ii) (High demand)

Region I: if  $k_2 < \theta \leq k_1$ , firm 1 bids at  $P$  whereas firm 2 submits bids no greater than  $P [\theta - k_2] / \theta$ .

Region II: if  $\theta > k_1$ , in any pure-strategy equilibrium firm  $i = 1, 2$  bids at  $P$  whereas firm  $j$  submits bids no greater than  $P [\theta - k_j] / \theta$ .

# Comparative Statics: Effects on Revenues

Symmetric costs and uniformly distributed demand

- ▶ Increasing capacity asymmetry

$k_1$	.5	.6	.7	.8	.9	1
$k_2$	.5	.4	.3	.2	.1	0
$E[R]$	.375	.420	.455	.480	.495	.5

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- ▶ Increasing aggregate capacity (symmetric capacities)

$K$	1	1.2	1.4	1.6	1.8	2
$E[R]$	.375	.320	.255	.180	.095	0

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- ▶ Reducing the price-cap  $P$

$P$	1	.9	0.75	.5	.25	0
$E[R]$	.375	.334	.281	.188	.094	0

# Symmetric Oligopoly

- ▶ Increasing the **number of (symmetric) firms** has a **pro-competitive effect**: the residual demand faced by any individual firm is smaller and hence the boundary between low and high demand realisations increases  $[\hat{\theta} = [N - 1] K / N]$ .
- ▶ With **multi-unit generators**, prices will tend to be higher than in the model in which these same units act independently.

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- ▶ The SMP will be a decreasing function of the number of owners, i.e. the industry concentration ratio.

# The Number of (symmetric) Firms

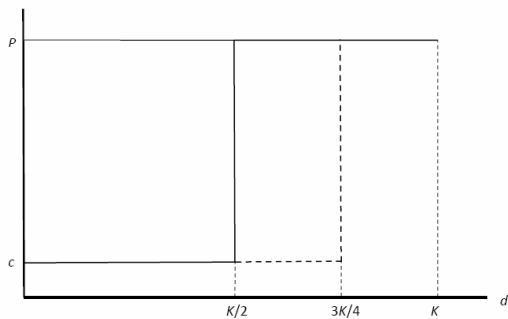


Figure 6: Equilibrium prices: two symmetric firms versus four symmetric firms

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**Relative incidence of low-demand states:**

- ▶ aggregate capacity (for given relative capacities across firms)
- ▶ number of firms
- ▶ symmetry in capacities (if symmetric costs)
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- ▶ the price-cap  $P$



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